

# Kinetic Monte Carlo–molecular dynamics investigations of hyperthermal copper deposition on Cu(111)

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Detailed kinetic Monte Carlo–molecular dynamics (KMC-MD) simulations of hyperthermal energy (10–100 eV) copper homoepitaxy reveal a reentrant layer-by-layer growth mode at low temperatures (50 K) and reasonable fluxes (1 ML/s, where ML stands for monolayer). This growth mode is the result of atoms with hyperthermal kinetic energies becoming inserted into islands when the impact site is near a step edge. The yield for atomic insertion as calculated with molecular dynamics near (111) step edges reaches a maximum near 18 eV. KMC-MD simulations of growing films find a minimum in the rms roughness as a function of energy near 25 eV. We find that the rms roughness saturates just beyond 0.5 ML of coverage in films grown with energies greater than 25 eV due to the onset of adatom-vacancy formation near 20 eV. Adatom-vacancy pairs increase the island nuclei density and the step-edge density, which increase the number of sites available to insert atoms. Smoothest growth in this regime is achieved by maximizing island and step-edge densities, which consequently reverses the traditional roles of temperature and flux: low temperatures and high fluxes produce the smoothest surfaces in these films. Dramatic increases in island densities are found to persist at room temperature, where island densities increase an order of magnitude from 20 to 150 eV.

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## I. INTRODUCTION

Recent technological advances have resulted in wide-ranging implementation of devices that utilize hyperthermal energy particles for thin-film and nanoscale device growth.<sup>1</sup> While these advances have propelled production efforts, a detailed understanding of the relevant physical mechanisms has not been fully developed. It has become increasingly apparent that even hyperthermal energetic particles can stimulate a variety of thermal and nonthermal processes, ranging from strain relaxation<sup>2</sup> to sputter erosion,<sup>3</sup> enhanced nuclei densities,<sup>4</sup> and improved composite layer adhesion.<sup>5</sup>

Efforts to model crystal surfaces during deposition have provided detailed information about the nature of surface kinetics. For example, molecular dynamics has allowed accurate predictions of many energy barriers for surface diffusion processes.<sup>6</sup> Many of these predictions have been carefully addressed experimentally,<sup>7–9</sup> but most efforts use deposition techniques with thermally generated constituents arriving at the substrate with less than a tenth of an eV.

Many of these studies have identified the “Ehrlich-Schwöebel”<sup>10,11</sup> barrier for interlayer diffusion as the source of three dimensional growth modes. The resulting “uphill” current produced by this interlayer diffusion barrier can be reduced by increasing temperature to surmount this barrier<sup>12,13</sup> or sufficiently decreasing step-step separation.<sup>14</sup> However, in heterostructures and nanostructures, elevated temperatures result in interdiffusion, chemical reaction, and thermodynamic relaxation, making nanoscale patterns difficult to retain.

Physical vapor deposition techniques utilizing hyperthermal energy constituents produce smoother epitaxial films in

many systems with finite Ehrlich-Schwöebel barriers.<sup>15,16</sup> It has been proposed that a “peening” effect known for building up stress at medium energies<sup>17–19</sup> may act as a relaxation mechanism at low and hyperthermal energies.<sup>20</sup>

Progress toward understanding hyperthermal energy collisions has been hindered by a lack of models that both accurately describe the collision process and the kinetic processes at realistic deposition rates ( $\sim 1$  ML/s). The kinetic Monte Carlo–molecular dynamics (KMC-MD) method allows the complexity of the atomic collision to be modeled uniquely with molecular dynamics for each atom without prior bias. Between deposition events, the kinetic Monte Carlo evolves the system using well-understood kinetics, until the next deposition event. Previous KMC-MD studies of platinum and silver were able to provide new insights into the role of the hyperthermal atom collision during growth.<sup>21</sup>

This paper presents results for energetic collisions on the Cu(111) surface: first, isolated molecular dynamics studies of atom impacts, and, second, KMC-MD simulations of entire films grown with hyperthermal energy atoms. A brief description of the simulation, improvements, and the energy barriers used for our simulations is presented first. The yields for various atomistic mechanisms resulting from molecular dynamics simulations of isolated impacts is presented next. The results of the full KMC-MD growth model at 50 K are then discussed. Finally, simulations of submonolayer films at room temperature are presented.

## II. SIMULATION DETAILS

Accurate modeling of crystal growth with hyperthermal energy atoms requires accurately modeling two classes of

TABLE I. EMT energy barriers in meV used in the KMC simulations have been calculated using ARTwork (Ref. 22). The details of the moves are discussed in detail elsewhere (Refs. 21 and 31). Edge diffusion events are atoms moving along the edge of an island. The “step” denotes whether the atom is moving along a (100) or (111) microfacet, *A* step or *B* step, respectively.  $N_i$  indicates the initial number of in-plane nearest neighbors (NN), and  $N_f$  the final.

				meV
<b>Terrace Diffusion</b>				
Adatom diffusion				54
Diffusion away from a step				525
Diffusion of dimers				117
Diffusion of vacancies				618
Dissociation from 1 NN				318
<b>Edge diffusion</b>	$N_i$	Step	$N_f$	
Corner of “A” island	1	<i>B</i>	1	179
Corner of “B” island	1	<i>A</i>	1	60
Corner diffusion	1	<i>A</i>	$\geq 1$	44
Corner diffusion	1	<i>B</i>	$\geq 1$	108
Step to corner	2	<i>A</i>	1	271
Step to corner	2	<i>B</i>	1	351
Step diffusion	2	<i>A</i>	$> 1$	228
Step diffusion	2	<i>B</i>	$> 1$	329
Kink to corner	3	<i>A</i>	1	496
Kink to corner	3	<i>B</i>	1	580
Kink to step	3	<i>A</i>	$> 1$	436
Kink to step	3	<i>B</i>	$> 1$	525
<b>Interlayer diffusion</b>				
Descent at straight step				167
Descent at <i>B</i> step kink				229

events active at times scales separated by about six orders of magnitude. The hyperthermal atom impact and subsequent thermalization process is complete in about 4 ps. On the other hand, the surface kinetics are active on the microsecond time scale. The technical challenge of accurately modeling sub-picosecond events for microseconds has been resolved by coupling two techniques, one appropriate for each time scale. Molecular dynamics is used to simulate the hyperthermal atom collisions, but is not feasible for modeling surface diffusion at realistic deposition rates. For the surface diffusion we use kinetic Monte Carlo, which passes atomic configurations at selected impact sites to the molecular dynamics, and accepts the new configurations following an impact. The full details of these simulations have been detailed elsewhere.<sup>21</sup>

We use a bowl-shaped molecular dynamics cluster with three classes of atoms: fully dynamic atoms nearest to the site of the impact, surrounded by three layers of dynamic Langevin atoms, and finally, an outer shell with four layers of static atoms. The Langevin coefficients and cell size are tuned to dissipate energy that can reflect from the boundary and lead to unrealistic rates for energetic reflection and adatom/vacancy formation.

We have found it useful to model isolated hyperthermal atom collisions with a few selected atomic configurations to

TABLE II. Additional effective medium energy barriers in meV used in the KMC-MD during 273 K simulations are presented. Energy barriers presented here are moves from highly coordinated sites, which were not included in low-temperature simulations since the rates for these moves are negligible at low temperatures.

Start	End	meV	<i>B</i> Step (if different)
<b>5 NN</b>	5 NN	606	
5 NN	4 NN	644	
5 NN	3 NN	692	
5 NN	2 NN	748	
<b>4 NN</b>	5 NN	448	
4 NN	4 NN	470	
4 NN	3 NN	502	
4 NN	2 NN	695	
4 NN	1 NN	681	
<b>3 NN</b>	5 NN	214	
3 NN	4 NN	291	
3 NN	3 NN	322	
3 NN	2 NN	436	525
3 NN	1 NN	496	580
3 NN	0 NN	748	
<b>2 NN</b>	5 NN	127	
2 NN	4 NN	~ 300	
2 NN	3 NN	~ 300	
2 NN	2 NN	228	329
2 NN	1 NN	271	351

develop a general picture of the atomic mechanisms important at various energies. Many atomic configurations on the surface can be classified according to the distance from a step-edge, so we have selected several positions near a (111) step-edge. We model 100 collisions in each of five atomic cells above a step-edge, the cell at the step-edge, and five cells below the step-edge for each energy of interest. For each collision, impact parameters are randomly selected, and the cluster evolved until the Langevin atoms have thermalized the system. The configuration is then frozen into a final state for analysis and saved. Once satisfactory statistics are developed at one position, the impact site is moved one atomic cell, and the process is repeated. We have found that the statistics for the fifth cell above or below is representative of all cells further from the step.

The role of the molecular dynamics during KMC-MD is the same, except that the configuration of atoms in the molecular dynamics cell is determined by the local environment of the impact site. The KMC uses a hexagonal lattice with in-plane periodic boundary conditions and a compliment of 23+ predefined thermal moves. Interstitial and hcp lattice positions are not allowed. The activation energies for these moves were calculated using ARTwork<sup>22</sup> and are listed in Table I. (For the 273 K simulations, the barriers in Table II are included as well.) Included in the KMC rate table is a flux weighted choice for adding new atoms. When the algorithm chooses to introduce a new atom, an impact site is

randomly selected. The local configuration of atoms is then copied into the molecular dynamics cluster, which simulates the collision. Once the final configuration is determined, it is returned to the KMC, and thermal evolution continues.

#### A. Modifications to the KMC-MD algorithm

One of the trickier parts of the KMC-MD method involves moving atoms from the continuous MD space to the discrete lattice of the KMC. During collisions involving many atoms on the surface, clusters of atoms occasionally freeze into hcp rather than fcc lattice positions. [hcp and fcc lattice positions are energetically equivalent on the (111) face using the effective medium theory potentials (EMT) for copper.] In the previous studies of platinum and silver,<sup>21</sup> these clusters rarely exceeded five atoms. As the algorithm encountered atoms in hcp sites, it would place them on the nearest available fcc site. During simulations of copper, these clusters are sometimes as large as eight atoms, and this previous technique did not always preserve the shape of the cluster. In some cases, atoms near the middle of a cluster could not be placed at all, since all nearby sites would already be filled.

Our modified algorithm creates a list of atoms in hcp sites, then sorts the list from highest coordination to the lowest. As each atom in the list is selected for placement, the three fcc sites surrounding that hcp site are checked for occupancy. The wayward atom is then placed into the unoccupied fcc site with the highest coordination (a random selection occurs if multiple sites have the highest coordination.) Since atoms near the center of a cluster get placed first, all atoms have an available fcc position. This change preserves the cluster shape and has successfully placed all the atoms in supported fcc sites.

### III. RESULTS FOR MD COLLISIONS

Simulating individual atomic collisions in a preselected environment can provide a general insight into the yields for atomic mechanisms at different energies. Once an impact has been simulated, the final atomic configuration is classified according to the change in the population of the atomic layers. If the impact site is above the step edge, and the incident atom is incorporated into the step, the event is considered an insertion. We do not distinguish between an atom that is actually inserted and one that just bounces over the step-edge. A decrease in the population of a layer requires the formation of a vacancy. The formation of vacancies usually provides additional adatoms (adatom-vacancy pairs) that can contribute to surface relaxation through enhanced lateral diffusion. If the total number of atoms in the cluster decreases, this is considered a sputtering event. (Spontaneous thermodynamic reevaporation is negligible.)

The yields averaged from many simulated collisions at several different atomic configurations are presented in Fig. 1. The hyperthermal atomic mechanisms observed in platinum and silver are present in copper, but the specific energies of activation vary somewhat. The insertion mechanism is active at the first position above the step-edge as low as 3 eV. As the energy increases, atoms are inserted deeper into

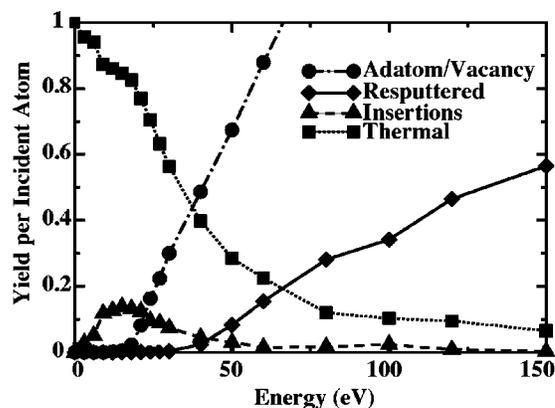


FIG. 1. Molecular dynamics simulations reveal a hierarchy of energetically activated nonequilibrium events, described in Sec. III. In order of increasing energy, the insertion mechanism is activated as low as 3 eV, followed by adatom-vacancy pair formation near 20 eV, and atomic resputtering near 40 eV.

the island, which increases the yield. At 9 eV, insertion events are observed four lattice positions into an island. The fifth atomic position into the step is not susceptible to insertion, so the insertion probability reaches a maximum at 15 eV. Above this energy, insertions continue to dominate beyond the first position above the step, but positions near the step become unstable and often form adatom-vacancy pairs.

Vacancy formation on the flat terrace begins abruptly near 20 eV, and the total yield increases at a rapid rate, reaching a yield of 1 at 60 eV. On average, more than two adatom-vacancy pairs are created per incident atom at 150 eV. At 80 eV, adatom-vacancy pairs have a higher probability at all the step positions considered than any other mechanism.

At about 40 eV, we begin to observe atoms escaping from the system, with some preference for positions close to the atomic step-edge. At low energies, an atom incident just above a step could shift the registry of atoms and become incorporated, but at higher energies the transverse momentum provided by the incident atom can eject step atoms from the system. The rapid increase in yields for adatom-vacancy pairs and sputtered atoms combine to double the number of dislodged atoms between 60 and 100 eV, greatly increasing the surface mobility and reducing the net growth rate to 65% of the incident flux. More comprehensive studies of resputtering have been reported elsewhere.<sup>23</sup>

### IV. RESULTS AND DISCUSSION OF 50 K KMC-MD DEPOSITION

While the molecular dynamics simulations of isolated impacts estimates the relative yields of different atomic mechanisms at various energies, a dynamically growing film requires the more sophisticated KMC-MD simulation. We have used KMC-MD to grow copper thin films on a Cu(111) surface using energies ranging from thermal to 40 eV. All the mechanisms identified with the isolated molecular dynamics in the preceding section are active, but the yield for resputtering below 40 eV is negligible.

Five examples of copper thin films grown with the KMC-MD are presented in Fig. 2. The films shown were

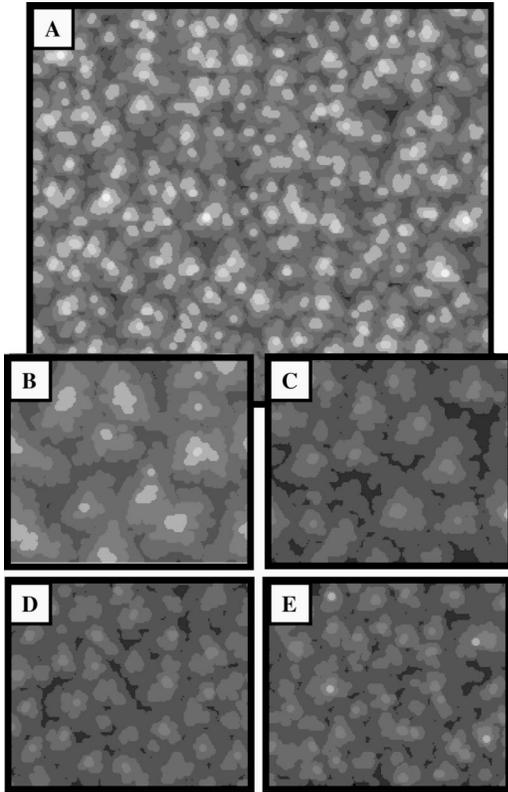


FIG. 2. Gray-scale images for KMC thermal deposition and four KMC-MD hyperthermal energy depositions are shown. (a) thermal, (b) 12 eV, (c) 21 eV, (d) 30 eV, and (e) 40 eV. All images have the same lateral length scales (atom size) and color maps. Films were grown at 1 ML/s on an  $80 \times 80$  lattice (thermal deposition used a  $150 \times 150$  lattice) using all the diffusion moves listed in Table I.

grown with a wide range of energies: thermal [Fig. 2(a)], 12 eV [Fig. 2(b)], 21 eV [Fig. 2(c)], 30 eV [Fig. 2(d)], and 40 eV [Fig. 2(e)]. All films described in this section are grown at  $\sim 50$  K at 1 ML/s deposition rate on a  $80 \times 80$  lattice, except thermal deposition that used a  $150 \times 150$  lattice. System sizes are selected to avoid finite size effects. All the images have the same lateral length scale and the same color map for ease of comparison (the size of an atom is the same in all the images, and the layer depths have the same color sequence in all images). While four monolayers of copper has been deposited in all cases, the films grown at 21 eV and 30 eV do not have any atom in the seventh and eighth layers. The thermally deposited film has a large population of atoms in these upper two layers, and is rougher than those grown with energetic deposition. The step density in the thermal films is much higher at 0.74 than the 21 eV or 30 eV films (0.39 and 0.45, respectively), corresponding to a shorter lateral length scale (step densities are discussed in more detail later).

A common way of representing smooth growth that establishes a connection with experimental efforts<sup>24,25</sup> is to plot the simulated antiphase Bragg intensities associated with reflection high-energy electron diffraction or x-ray diffraction. Antiphase intensities will exhibit complete oscillations between 0 and 1 for perfect layer-by-layer growth, and a monotonic decay for three-dimensional roughening. Due to

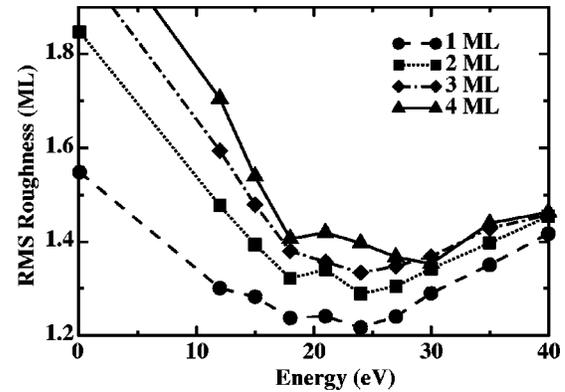


FIG. 3. The rms roughness at the completion of each monolayer shows a minimum near 25 eV. As the film grows thicker, the minima are observed to shift toward higher energies. Beyond 1 ML of coverage, the roughness of films grown with energies above 25 eV increases slower than films grown with lower energies. The time evolution of the rms roughness is shown in more detail in Fig. 4.

space constraints, we have limited the presentation of simulated antiphase intensity data to our discussion of temperature and flux in Sec. V. With the exception of thermally deposited films, all the films studied exhibited layer-by-layer oscillations of varying strengths. The antiphase intensity of the thermally grown film decays monotonically in this low-temperature regime, consistent with the experimental observation.<sup>26</sup> The antiphase intensity oscillations are strongest between 20 and 30 eV, corresponding with the minima in roughness shown in Fig. 3.

The roughness of the KMC-MD films is quantified by calculating the rms roughness at the completion of each of the four monolayers deposited. These roughness data as a function of the deposition energy are shown in Fig. 3. Even after depositing only one monolayer, the films grown with atoms in the 20 eV range have a much lower roughness than those grown with higher or lower energies. As the film progresses, this minimum roughness appears to shift toward higher energies. The roughness of films grown with less than 25 eV grows more quickly after 1 ML of coverage than the roughness of the films grown with energies greater than 25 eV. Careful examination of the 40 eV data reveals very little change in the surface roughness after the first monolayer.

The time evolution of the rms roughness is shown in greater detail for a few selected energies in Fig. 4. The rms roughness for the thermally deposited film diverges as a power law, as expected.<sup>27</sup> For all energies, the rms roughness grows rapidly until about 0.5 ML. Below 0.5 ML, films deposited with energies greater than 20 eV actually develop roughness faster than the thermally deposited film. As the hyperthermal beam creates large numbers of adatom vacancy pairs, the surface width increases rapidly, but these extra adatoms in turn increase nuclei densities, which contribute to higher step densities, shown in Fig. 5.

Island density and step density (top panels), as well as time-averaged insertion and vacancy yields (bottom panels) are presented in Figs. 5(a–c) for 12 eV, 27 eV, and 40 eV, respectively. As the energy increases from 12 eV to 40 eV, the saturation island density (approximately the density at 0.15 ML) increases by a factor of 6. Since the island density

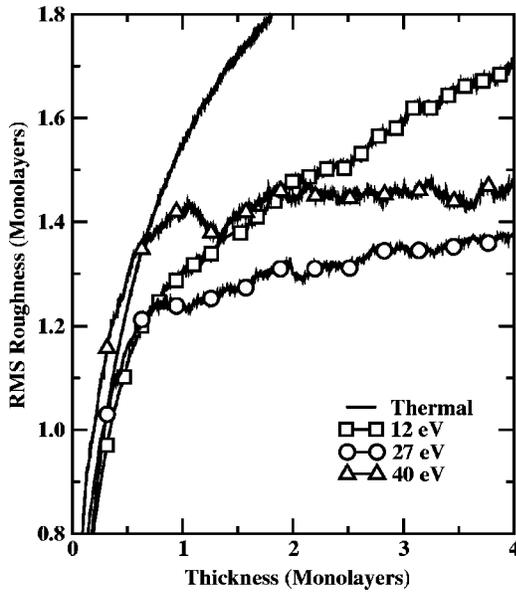


FIG. 4. The rms roughness as a function of time is presented for four characteristic energies. During thermal deposition, the rms roughness increases steadily over the entire range studied. At hyperthermal energies, the roughness is observed to grow more slowly after 0.5 ML. For films grown with 27 and 40 eV particles, the roughness grows very slowly above 1 ML, compared to thermal deposition.

and the average island size are related ( $N_x = \theta/\bar{s}$ , where  $\theta$  is the coverage and  $\bar{s}$  is the average island size), one might naively expect a factor of 6 increase in island density to correspond with a  $\sqrt{6}$  increase in the step density at constant coverage. In actuality, the increase in island density does not translate directly to an increase in step-edge density, the step-edge density in Fig. 5 increases by only about 50%, not  $\sqrt{6}$ . This is partly a consequence of our definition of step density. We define the step density as the number of atoms with empty neighbor sites, since the insertion mechanism relies on displacing an atom into an empty neighboring lattice position. This definition can decouple island density and step density. For example, if all islands were composed of four atoms, the step density would be four times the island density. But if all the islands were made from dimers, the step density would be the same, but the island density would increase by a factor of 2.

Figure 5 also displays the dynamic yields for the insertion mechanism and the formation of vacancies at 12 eV [Fig. 5(a)], 27 eV [Fig. 5(b)], and 40 eV [Fig. 5(c)]. While the yields discussed in the preceding section and presented in Fig. 1 provide an average yield for insertions and vacancies at a given energy near a (111) step edge, the yields in Fig. 5 are dynamic. Each line shape is a running average over a few hundredths of a monolayer in coverage. The yields for insertions and vacancy production are observed to be sensitive to fluctuations in the surface structure.

The insertion yields at 12 eV and 27 eV track the step density very closely. At very short times, while the surface is still very flat, the step density is very low and few sites are available for insertion. During these times, the vacancy yield

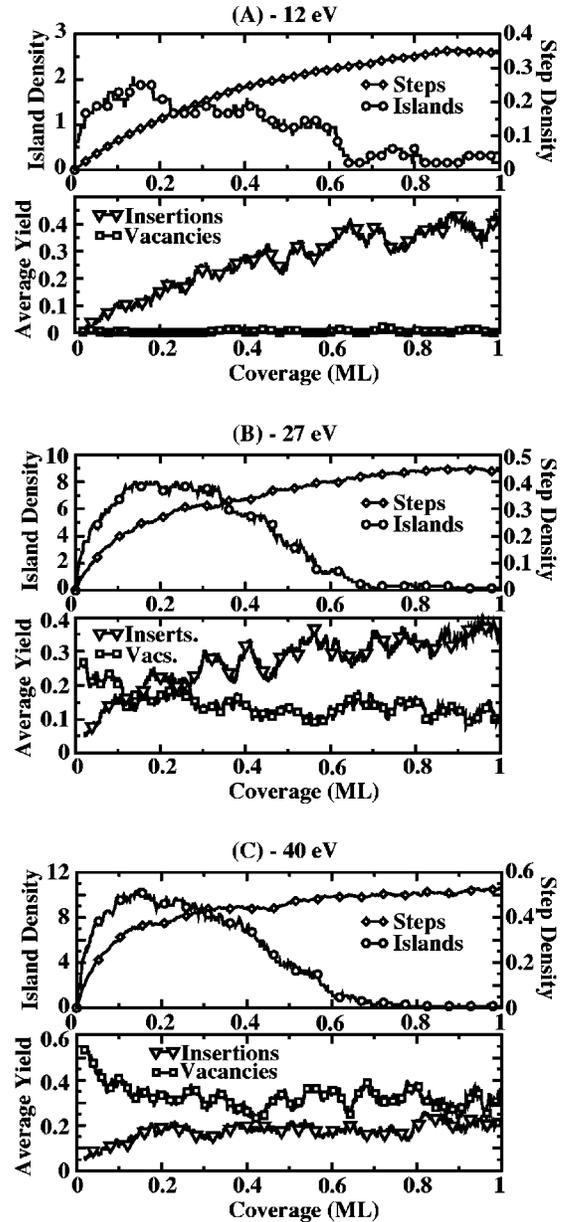


FIG. 5. The atomic configuration of the surface determines the relative yields of mechanisms activated by the incident atom beam. For each of three energies, 12 eV (a), 27 eV (b), and 40 eV (c), the top panels show the island and step densities while the bottom panels show the time-averaged yields for insertion and adatom-vacancy production. Beyond the first monolayer, these values reach equilibrium and change very little about the 1 ML value.

is large, which in turn increases the island and step densities. With increasing step density, more sites become available for insertion, increasing the insertion yield. At these energies, adatom-vacancy production is suppressed at step-edges. So, as the surface becomes more populated with islands and fewer flat terraces, the vacancy yield decreases. At about 0.3 ML, islands begin to coalesce and decrease the number of first-layer step-edges. The formation of adatom-vacancy pairs on the second layer (atop islands) keeps the step-edge density high, and the insertion mechanism does not suffer.

The increase in the island density and corresponding in-

crease in the step density below 0.5 ML in the 27 and 40 eV simulations sets the stage for smooth growth at later times. The drop in the island density to a very low value by 0.7 ML indicates near completion of the first layer before second-layer growth. The abrupt change in the rms roughness (Fig. 4) near 0.5 ML of coverage illustrates the predicted benefit of using hyperthermal energy particles. With increasing particle energy, the rms roughness grows more slowly until, at 40 eV, the rms roughness does not perceptibly increase above 1 ML of coverage. This “saturated” roughness was observed in all films grown with energies at or above 30 eV. While the roughness does not noticeably increase above 1 ML in these films, higher incidence energies result in larger saturation roughnesses.

The effect of a saturated roughness is the result of the insertion yield and the vacancy yield, both achieving saturation. At 27 eV, the first four lattice positions immediately above a step-edge are available for insertion, which suppresses vacancy formation. As a result, insertions have a higher yield during growth above 0.5 ML than vacancies [Fig. 5(b)], and the saturation roughness is less than at 40 eV. At higher energies, the first lattice position above the step is unstable upon impact. As a result, the balance of insertion and vacancy yields falls in favor of vacancies at 40 eV [see Fig. 5(c)], and notice the scale differences between 12 eV [Fig. 5(a)], 27 eV [Fig. 5(b)], and 40 eV [Fig. 5(c)].

While total insertions decrease at 40 eV, other energetic effects begin to compensate and keep the roughness from increasing dramatically. For example, the increasing incident energy can break islands into smaller pieces, preventing an additional layer from nucleating on top of it. Atom impacts on top of multiple layers can lead to collective downward mobility, e.g. at 40 eV, two atoms or more were observed to fall in the layer beneath the impact site one time in 25. These and other mechanisms that involve collective motion of multiple atoms have been discussed in detail elsewhere.<sup>28,29</sup>

The large insertion yield effectively reduces the interlayer diffusion barrier by providing an alternative to thermal descent for crossing the step. We have performed KMC simulations using an reduced interlayer diffusion barrier to mimic this effect. This oversimplification fails to reproduce the correct line shape for the rms roughness and does not provide a layer-by-layer type growth, underscoring the importance of adatom-vacancy pairs. The adatom-vacancy pairs contribute to establishing a microscopically rough interface that sustains a macroscopically smooth growth front through high insertion yields.

To review, as a film begins to grow with atoms in the 25 eV energy range, the surface initially becomes pocked with vacancies. The deposited atoms combine with adatoms from adatom-vacancy pairs to develop high densities of small islands, which have low probabilities for second layer nucleation. Both the vacancies and the new islands increase the step-edge density, which leads to high insertion yields. As the islands grow from insertion and aggregation, some begin to form second-layer islands and obtain vacancies prior to coalescence. This establishes an average distance between step-edges of about three atomic positions, and the roughness saturates. As the vacancies are filled and new levels are

nucleated, the surface grows smoothly with a constant roughness. This smooth growth relies on both the insertions to keep islands growing, and on the vacancies to provide additional adatoms and to reduce the area available for new layer nucleation.

## V. NONINTUITIVE ROLE OF TEMPERATURE AND FLUX IN ENERGETIC DEPOSITION

During thermal homoepitaxy, the roles of temperature and flux are well understood,<sup>26</sup> smooth growth occurs when adatoms have enough time to diffuse to an existing island and the islands have time to coalesce before second-layer nucleation occurs. This is most likely to occur when the temperature is increased to increase the diffusion length, and the flux decreased to reduce the probability of nucleating a new island before coalescence.

During hyperthermal energy deposition, this phenomenology reverses due to the strong dependence on step density. Other authors have found that the best results for smooth growth with hyperthermal deposition can be obtained by maximizing the nuclei density.<sup>12,13</sup> Since island densities scale as  $N_x \propto (F/D)^p$  ( $F$  is flux,  $D$  is the temperature-dependent diffusivity, and  $p$  depends on the critical nuclei size),<sup>30</sup> establishing a high density of islands requires decreasing the temperature and increasing the flux. A high island density also means a small average island size ( $N_x = \theta/\bar{s}$ , where  $\theta$  is the film coverage and  $\bar{s}$  is the average island size), reducing the target area for second-layer nucleation and keeping the entire second layer surface close to a step-edge. A hyperthermal atom incident on the top of one of these islands has a very high probability of inserting, rather than relying on kinetic diffusion to cross to the lower terrace.

We have presented rms roughness as a function of time and antiphase intensity data for films grown with 24 eV atoms at various temperatures and flux in Fig. 6. Contrary to thermal deposition,<sup>26</sup> the rougher films occur with the higher temperatures and lower fluxes. In addition, one can compensate for a decrease in flux by decreasing the temperature. For example, the surface grown at 50 K and 0.1 ML/s was much rougher than the film grown at 50 K and 1 ML/s, but at 35 K with 0.1 ML/s flux, the film grows smoothly.

## VI. HYPERTHERMAL ENERGY INDUCED ISLAND DENSITIES

While atomic insertion provides a compelling mechanism for controlling surface roughness, the extremely small island sizes and high step densities required for layer-by-layer behavior reduce the effectiveness at temperatures typical for film growth. At typical deposition temperatures, the average island size becomes large enough to reduce the number of sites available for insertion significantly, in turn reducing the average insertion yield. Even though the insertion yield drops, the adatom-vacancy pairs generated by hyperthermal energy ion beams provide additional adatoms that increase island densities.

The maximum island density achieved by the time the first layer accumulates 0.15 ML of material is shown for

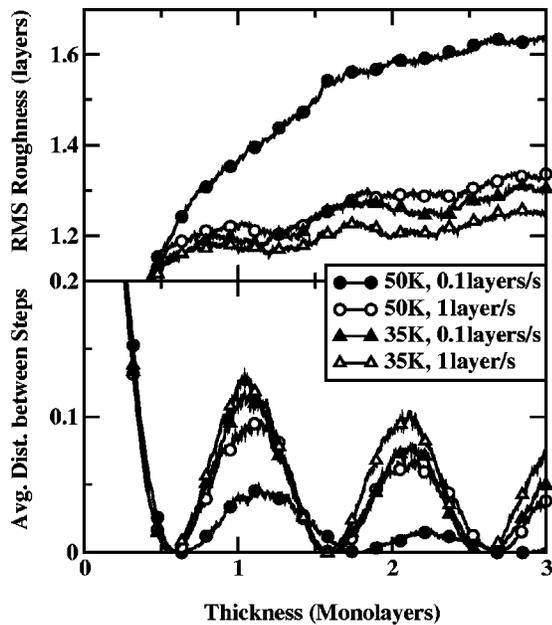


FIG. 6. In this reentrant layer-by-layer mode, the roles of temperature and flux are reversed: high flux and low temperatures yield the smoothest films, as opposed to thermal deposition. Shown here are films grown at 0.1 ML/s and 1 ML/s flux, and at 35 K and 50 K. The top panel shows the RMS roughness of each of the four films and the bottom panel is the simulated antiphase intensity. The roughness of films grown at 35 K and 1 ML/s is 50% of the value for films grown at 50 K with 0.1 ML/s, with antiphase intensity maxima more than three times as intense. The reversal of roles is a consequence of relying on the insertion mechanism for smooth growth, which requires high step densities to be effective.

films grown at 50 K and 273 K in Fig. 7. The 273 K deposition is performed on a  $400 \times 400$  lattice at 100 ML/s using all the diffusion moves listed in Tables I and II. Increased adatom density due to adatom-vacancy production leads to dramatic increases in the island density at both temperatures. The onset of sputter erosion near 40 eV acts to slow the net growth speed relative to the nucleation rate, increasing the effective flux. As material in the substrate is lost to sputter erosion, saturation island densities (typically at about 0.15 ML of coverage) are reached as low as 0.05 ML. As atoms are deposited or displaced, the first layer collects most of the deposited material, nucleating new islands while the additional vacancies produced by the sputter erosion reduce the net material deposited. For example, consider an energy at which two adatom-vacancy pairs are produced and the sputter yield is 0.5. On average, every incident atom will create 2.5 atoms in the first layer, while only depositing 0.5 atoms in total. After 0.1 ML of *net* deposition, the first layer will have almost 0.25 ML coverage.

The data presented in Fig. 7 is the density of islands after the *first* layer has reached 0.15 ML of coverage, not 0.15 ML of total deposition. The saturation island density depends on the coverage in the layer being considered, not on the total amount of material deposited. It may be surprising that such a strong effect remains at 273 K, as the thermal activation of diffusion increases the probability for adatom-vacancy recombination. We find that the high adatom densities lead to

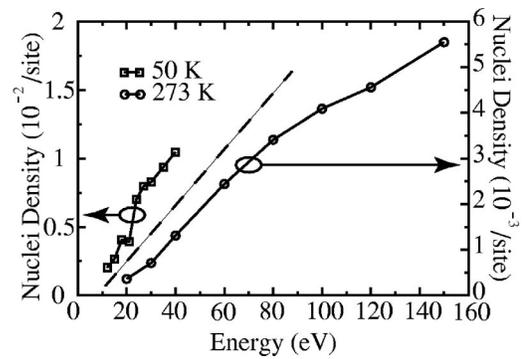


FIG. 7. With increasing energy, large yields of adatom-vacancy pairs raise the free adatom density, which in turn increases the island density. This effect is observed both at 50 K and at room temperature, where the island density increases by more than an order of magnitude with 150 eV of energy. Plotted here is the maximum island density achieved up to 0.15 ML of coverage for 50 K deposition (squares are for left axis scale) at 1 ML/s and 273 K deposition (circles are for right axis scale) at 100 ML/s.

rapid formation of dimers, which still move freely with only a 117 meV diffusion barrier. Dimer step crossing is negligible, and dimer breakup occurs infrequently.

We have also found that high island densities are maintained with unexpectedly low average island sizes due to islands being “chipped” by incident atoms. While large islands are occasionally broken into two smaller stable islands, breaking dimers and adatoms off of stable islands occurs with a relatively high yield, of the order of one chipping event for every ten impacts on an island. This contributes to additional nucleation of small islands and suppresses the growth of large islands.

The significance of enhanced nuclei densities has already been experimentally demonstrated by using an ion beam to increase the free adatom density at the beginning of each monolayer of growth while depositing copper on Cu(111).<sup>13</sup> (In this example, a separate 1.2 keV argon ion beam and a flux of thermal atoms were used.) The ability to dramatically increase nuclei densities using a single growth beam in the room temperature regime opens new possibilities for circumventing three-dimensional growth. It is possible that pulsing the final beam energy between low energy ( $\sim 20$  eV) and high energy ( $\sim 100$  eV) in a manner similar to the previous example<sup>13</sup> can allow the benefits of high island density and atomic insertion to be utilized while using a single deposition source.

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- <sup>1</sup>T. Minvielle, R. White, and R. Wilson, *J. Appl. Phys.* **79**, 5116 (1996).
- <sup>2</sup>B. Karr, Y. Kim, I. Petrov, D. Bergstrom, D. Cahill, J. Greene, L. Madsen, and J. Sundgren, *J. Appl. Phys.* **80**, 6699 (1996).
- <sup>3</sup>T. Michely and C. Teichert, *Phys. Rev. B* **50**, 11 156 (1994).
- <sup>4</sup>S. Esch, M. Breeman, M. Morgenstern, T. Michely, and G. Comsa, *Surf. Sci.* **365**, 187 (1996).
- <sup>5</sup>H. Fladry, N. Tegen, and G. Wolf, *Nucl. Instrum. Methods Phys. Res. B* **91**, 575 (1994).
- <sup>6</sup>P. Stolze, *J. Phys.: Condens. Matter* **6**, 9495 (1994).
- <sup>7</sup>K. Morgenstern, G. Rosenfeld, and G. Comsa, *Phys. Rev. Lett.* **76**, 2113 (1996).
- <sup>8</sup>G. Rosenfeld, K. Morgenstern, I. Beckmann, W. Wulfhekel, E. Laegsgaard, F. Besenbacher, and G. Comsa, *Surf. Sci.* **402-404**, 401 (1998).
- <sup>9</sup>M. Geisen and G.S. Icking-Konert, *Surf. Sci.* **412/413**, 645 (1998).
- <sup>10</sup>F.H.G. Ehrlich, *J. Chem. Phys.* **44**, 1039 (1966).
- <sup>11</sup>R. Schwöbel and E. Shipsey, *J. Appl. Phys.* **37**, 3682 (1966).
- <sup>12</sup>G. Rosenfeld, N. Lipkin, W. Wulfhekel, J. Kliewer, K. Morgenstern, B. Poelsema, and G. Comsa, *Appl. Phys. A: Mater. Sci. Process.* **61**, 455 (1995).
- <sup>13</sup>W. Wulfhekel, N. Lipkin, J. Kliewer, G. Rosenfeld, L. Jorritsma, B. Poelsema, and G. Comsa, *Surf. Sci.* **348**, 227 (1996).
- <sup>14</sup>M. Geisen and H. Ibach, *Surf. Sci.* **431**, 109 (1999).
- <sup>15</sup>S. Esch, M. Bott, T. Michely, and G. Comsa, *Appl. Phys. Lett.* **67**, 3209 (1995).
- <sup>16</sup>Y. Gotoh, H. Yoshii, T. Amioka, K. Kameyama, H. Tsuji, and J. Ihsikawa, *Thin Solid Films* **288**, 300 (1996).
- <sup>17</sup>S.-S. Sun, *J. Vac. Sci. Technol. A* **4**, 572 (1986).
- <sup>18</sup>H. Windischmann, *J. Appl. Phys.* **62**, 1800 (1987).
- <sup>19</sup>H. Windischmann, *Crit. Rev. Solid State Mater. Sci.* **17**, 547 (1992).
- <sup>20</sup>M. Koster and H.M. Urbassek, *Phys. Rev. B* **63**, 224111 (2001).
- <sup>21</sup>J. Jacobsen, B. Cooper, and J. Sethna, *Phys. Rev. B* **58**, 15 847 (1998).
- <sup>22</sup>P. Stolze, *Simulation Methods in Atomic-Scale Materials Physics* (Polyteknisk Forlag, Denmark, 1997). Dr. Stolze has made code and manuals available online at the following web address: <http://www.aue.auc.dk/~stolze/art.html>
- <sup>23</sup>X. Zhou and H. Wadley, *Surf. Sci.* **431**, 58 (1999).
- <sup>24</sup>B. Poelsema, A. Becker, R. Kunkel, G. Rosenfeld, L. Verheij, and G. Comsa, in *Surface Science Principles and Applications*, edited by R. Howe, R. Lamb, and K. Wandelt (Springer-Verlag, Berlin, 1993), p. 95.
- <sup>25</sup>T. Michely, M. Kalff, and G. Comsa, in *Mechanisms and Principles of Epitaxial Growth in Metallic Systems*, edited by L. T. Wille, C. P. Burmester, K. Terakura, G. Comsa, and E. D. Williams, *Mater. Res. Soc. Symp. Proc.* 528 (Materials Research Society, Pittsburgh, 1998).
- <sup>26</sup>G. Rosenfeld, B. Poelsema, and G. Comsa, *The Chemical Physics of Solid Surfaces: Growth and Properties of Ultrathin Epitaxial Layers* (Elsevier Science, New York, 1997), Chap. 3.
- <sup>27</sup>F. Family, *Universalities in Condensed Matter* (Springer-Verlag, Berlin, 1988), p. 193.
- <sup>28</sup>A. Voter, *J. Chem. Phys.* **106**, 4665 (1997).
- <sup>29</sup>X. Zhou and H. Wadley, *Surf. Sci.* **430**, 42 (1999).
- <sup>30</sup>J. Venables, G. Spiller, and M. Hanbücken, *Rep. Prog. Phys.* **47**, 399 (1984).
- <sup>31</sup>J. Jacobsen, K. Jacobsen, and J. Norkskov, *Surf. Sci.* **359**, 37 (1996).